

ROBERT SEDGEWICK | KEVIN WAYNE

<http://algs4.cs.princeton.edu>

## 3.4 HASH TABLES

---

- ▶ *hash functions*
- ▶ *separate chaining*
- ▶ *linear probing*
- ▶ *context*

# Symbol table implementations: summary

implementation	guarantee			average case			ordered ops?	key interface
	search	insert	delete	search hit	insert	delete		
<b>sequential search (unordered list)</b>	$N$	$N$	$N$	$\frac{1}{2}N$	$N$	$\frac{1}{2}N$		<code>equals()</code>
<b>binary search (ordered array)</b>	$\lg N$	$N$	$N$	$\lg N$	$\frac{1}{2}N$	$\frac{1}{2}N$	✓	<code>compareTo()</code>
<b>BST</b>	$N$	$N$	$N$	$1.39 \lg N$	$1.39 \lg N$	$\sqrt{N}$	✓	<code>compareTo()</code>
<b>red-black BST</b>	$2 \lg N$	$2 \lg N$	$2 \lg N$	$1.0 \lg N$	$1.0 \lg N$	$1.0 \lg N$	✓	<code>compareTo()</code>

Q. Can we do better?

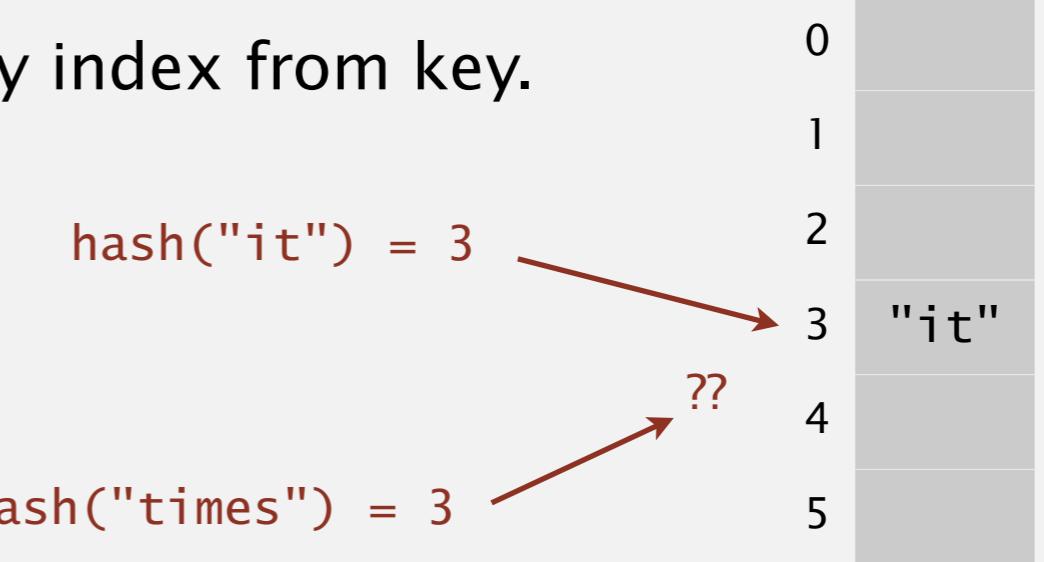
A. Yes, but with different access to the data.

# Hashing: basic plan

---

Save items in a **key-indexed table** (index is a function of the key).

**Hash function.** Method for computing array index from key.



**Issues.**

- Computing the hash function.
- Equality test: Method for checking whether two keys are equal.
- Collision resolution: Algorithm and data structure to handle two keys that hash to the same array index.

**Classic space-time tradeoff.**

- No space limitation: trivial hash function with key as index.
- No time limitation: trivial collision resolution with sequential search.
- Space and time limitations: hashing (the real world).

# Algorithms

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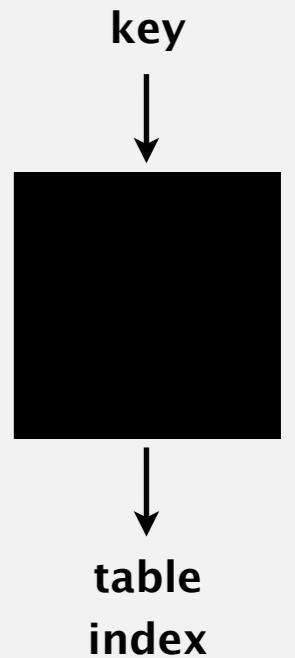
# Computing the hash function

---

Idealistic goal. Scramble the keys uniformly to produce a table index.

- Efficiently computable.
- Each table index equally likely for each key.

thoroughly researched problem,  
still problematic in practical applications



Ex 1. Phone numbers.

- Bad: first three digits.
- Better: last three digits.

Ex 2. Social Security numbers.

- Bad: first three digits.
- Better: last three digits.

573 = California, 574 = Alaska  
(assigned in chronological order within geographic region)

Practical challenge. Need different approach for each key type.

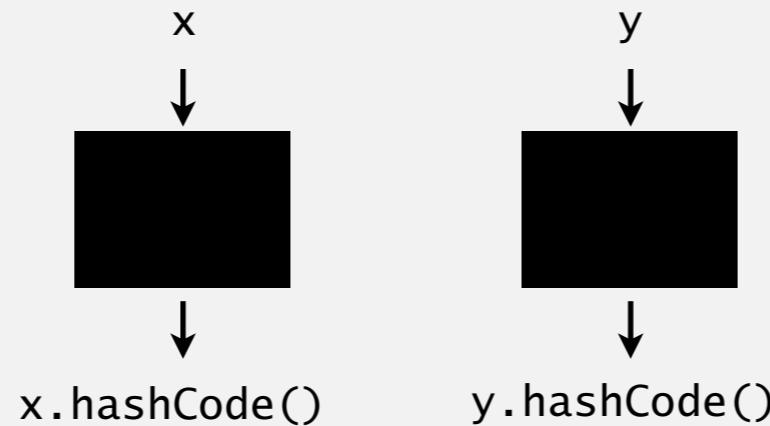
# Java's hash code conventions

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All Java classes inherit a method `hashCode()`, which returns a 32-bit `int`.

**Requirement.** If `x.equals(y)`, then `(x.hashCode() == y.hashCode())`.

**Highly desirable.** If `!x.equals(y)`, then `(x.hashCode() != y.hashCode())`.



**Default implementation.** Memory address of `x`.

**Legal (but poor) implementation.** Always return 17.

**Customized implementations.** `Integer`, `Double`, `String`, `File`, `URL`, `Date`, ...

**User-defined types.** Users are on their own.

# Implementing hash code: integers, booleans, and doubles

## Java library implementations

```
public final class Integer
{
    private final int value;
    ...
    public int hashCode()
    {   return value;   }
}
```

```
public final class Boolean
{
    private final boolean value;
    ...
    public int hashCode()
    {
        if (value) return 1231;
        else       return 1237;
    }
}
```

```
public final class Double
{
    private final double value;
    ...
    public int hashCode()
    {
        long bits = doubleToLongBits(value);
        return (int) (bits ^ (bits >>> 32));
    }
}
```

convert to IEEE 64-bit representation;  
xor most significant 32-bits  
with least significant 32-bits

Warning: -0.0 and +0.0 have different hash codes

# Implementing hash code: strings

## Java library implementation

```
public final class String
{
    private final char[] s;
    ...
    public int hashCode()
    {
        int hash = 0;
        for (int i = 0; i < length(); i++)
            hash = s[i] + (31 * hash);
        return hash;
    }
}
```

A red arrow points from the text "j<sup>th</sup> character of s" to the expression `s[i]` in the code.

char	Unicode
...	...
'a'	97
'b'	98
'c'	99
...	...

- Horner's method to hash string of length  $L$ :  $L$  multiplies/adds.
  - Equivalent to  $h = s[0] \cdot 31^{L-1} + \dots + s[L-3] \cdot 31^2 + s[L-2] \cdot 31^1 + s[L-1] \cdot 31^0$ .

**Ex.**      String s = "call";

```
int code = s.hashCode();
```

$$\begin{array}{r}
 \leftarrow \quad 3045982 = 99 \cdot 31^3 + 97 \cdot 31^2 + 108 \cdot 31^1 + 108 \cdot 31^0 \\
 \qquad\qquad\qquad = 108 + 31 \cdot (108 + 31 \cdot (97 + 31 \cdot (99))) \\
 \qquad\qquad\qquad \text{(Horner's method)}
 \end{array}$$

# Implementing hash code: strings

## Performance optimization.

- Cache the hash value in an instance variable.
- Return cached value.

```
public final class String
{
    private int hash = 0;                                ← cache of hash code
    private final char[] s;
    ...

    public int hashCode()
    {
        int h = hash;
        if (h != 0) return h;                            ← return cached value
        for (int i = 0; i < length(); i++)
            h = s[i] + (31 * h);
        hash = h;                                       ← store cache of hash code
        return h;
    }
}
```

Q. What if hashCode() of string is 0?

# Implementing hash code: user-defined types

```
public final class Transaction implements Comparable<Transaction>
{
    private final String who;
    private final Date when;
    private final double amount;

    public Transaction(String who, Date when, double amount)
    { /* as before */ }

    ...

    public boolean equals(Object y)
    { /* as before */ }

    public int hashCode()
    {
        int hash = 17;           ← nonzero constant
        hash = 31*hash + who.hashCode(); ← for reference types,
                                         use hashCode()
        hash = 31*hash + when.hashCode(); ← for primitive types,
                                         use hashCode()
        hash = 31*hash + ((Double) amount).hashCode(); ← of wrapper type
        return hash;
    }
}
```

nonzero constant

for reference types,  
use hashCode()

for primitive types,  
use hashCode()  
of wrapper type

typically a small prime

# Hash code design

---

"Standard" recipe for user-defined types.

- Combine each significant field using the  $31x + y$  rule.
- If field is a primitive type, use wrapper type `hashCode()`.
- If field is `null`, return 0.
- If field is a reference type, use `hashCode()`.  applies rule recursively
- If field is an array, apply to each entry.  or use `Arrays.deepHashCode()`

In practice. Recipe works reasonably well; used in Java libraries.

In theory. Keys are bitstring; "universal" hash functions exist.

Basic rule. Need to use the whole key to compute hash code;  
consult an expert for state-of-the-art hash codes.

# Modular hashing

Hash code. An int between  $-2^{31}$  and  $2^{31} - 1$ .

Hash function. An int between 0 and  $M - 1$  (for use as array index).

typically a prime or power of 2

```
private int hash(Key key)
{   return key.hashCode() % M; }
```

bug

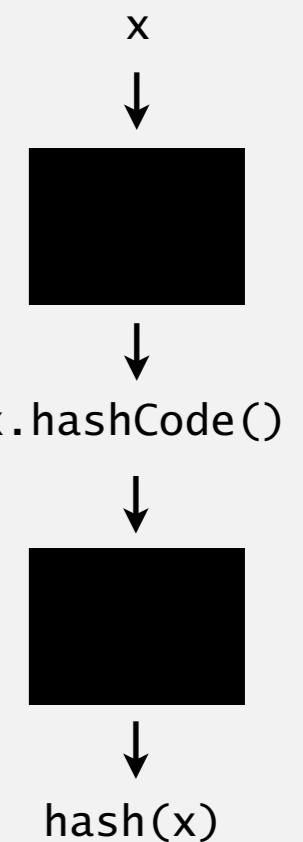
```
private int hash(Key key)
{   return Math.abs(key.hashCode()) % M; }
```

1-in-a-billion bug

hashCode() of "polygenelubricants" is  $-2^{31}$

```
private int hash(Key key)
{   return (key.hashCode() & 0xffffffff) % M; }
```

correct

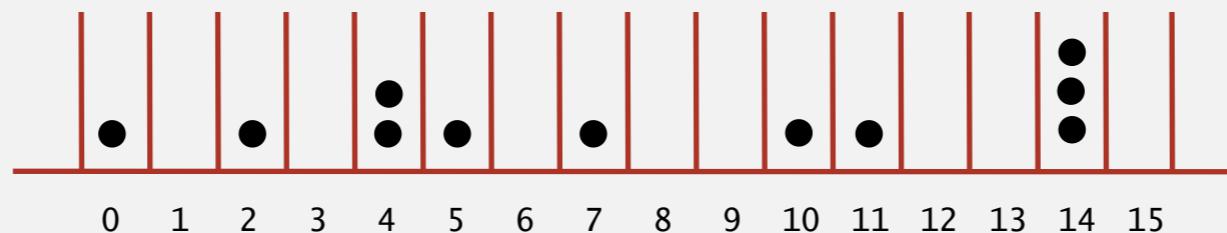


## Uniform hashing assumption

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**Uniform hashing assumption.** Each key is equally likely to hash to an integer between 0 and  $M - 1$ .

**Bins and balls.** Throw balls uniformly at random into  $M$  bins.



**Birthday problem.** Expect two balls in the same bin after  $\sim \sqrt{\pi M / 2}$  tosses.

**Coupon collector.** Expect every bin has  $\geq 1$  ball after  $\sim M \ln M$  tosses.

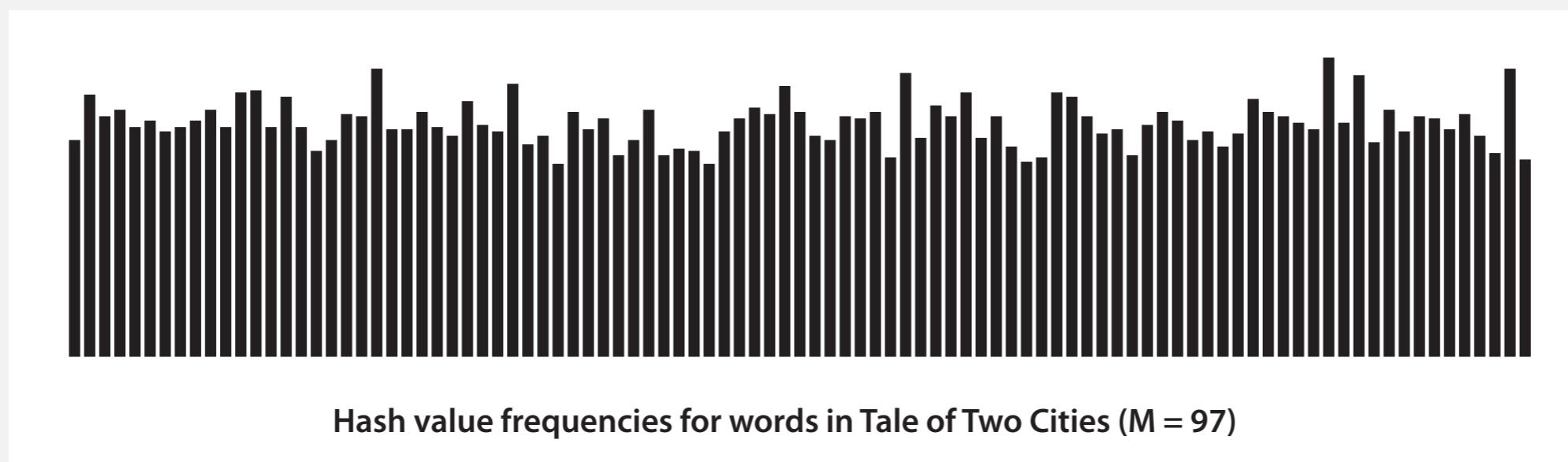
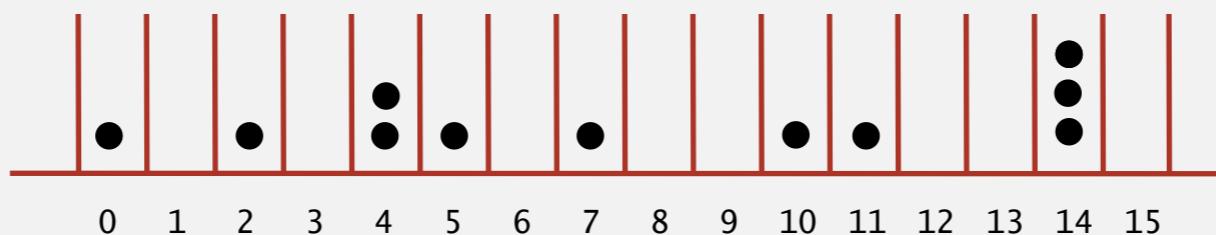
**Load balancing.** After  $M$  tosses, expect most loaded bin has  $\Theta(\log M / \log \log M)$  balls.

# Uniform hashing assumption

---

**Uniform hashing assumption.** Each key is equally likely to hash to an integer between 0 and  $M - 1$ .

**Bins and balls.** Throw balls uniformly at random into  $M$  bins.



Java's String data uniformly distribute the keys of Tale of Two Cities

# Algorithms

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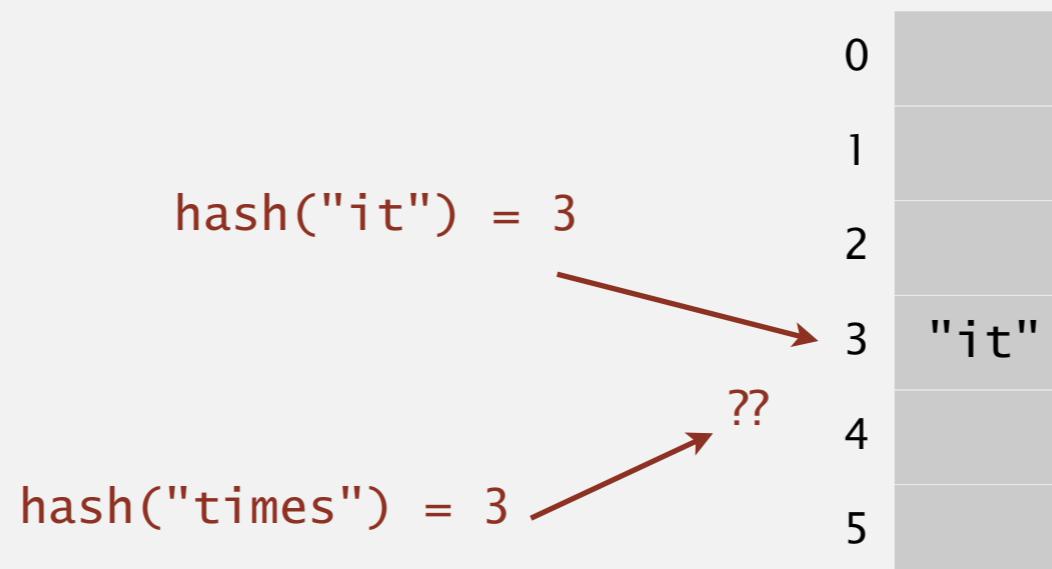
- ▶ *hash functions*
- ▶ ***separate chaining***
- ▶ *linear probing*
- ▶ *context*

# Collisions

---

**Collision.** Two distinct keys hashing to same index.

- Birthday problem  $\Rightarrow$  can't avoid collisions unless you have a ridiculous (quadratic) amount of memory.
- Coupon collector + load balancing  $\Rightarrow$  collisions are evenly distributed.

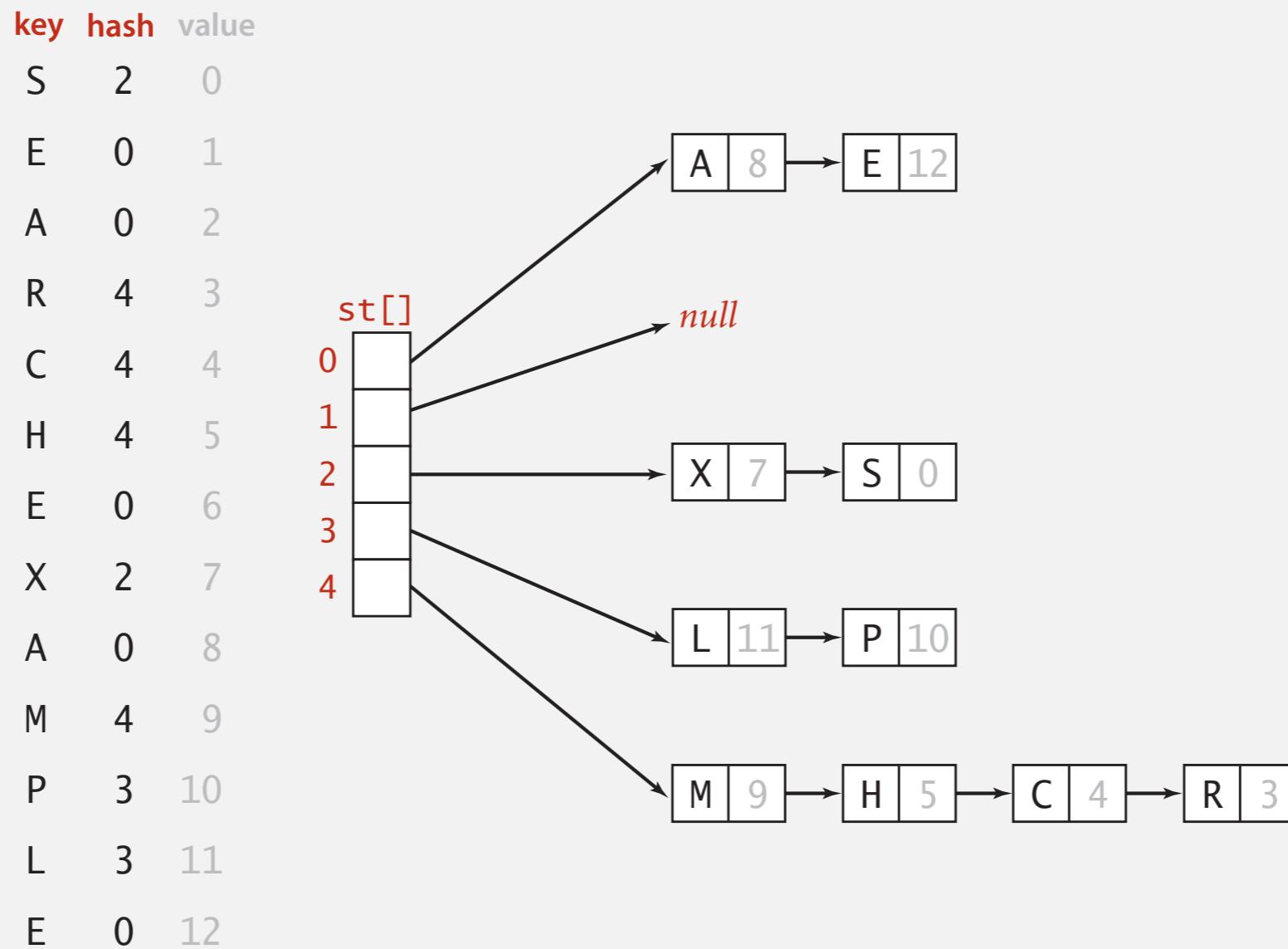


**Challenge.** Deal with collisions efficiently.

# Separate-chaining symbol table

Use an array of  $M < N$  linked lists. [H. P. Luhn, IBM 1953]

- Hash: map key to integer  $i$  between 0 and  $M - 1$ .
- Insert: put at front of  $i^{\text{th}}$  chain (if not already there).
- Search: need to search only  $i^{\text{th}}$  chain.



# Separate-chaining symbol table: Java implementation

```
public class SeparateChainingHashST<Key, Value>
{
    private int M = 97;                      // number of chains
    private Node[] st = new Node[M]; // array of chains

    private static class Node
    {
        private Object key; ← no generic array creation
        private Object val; ← (declare key and value of type Object)
        private Node next;
        ...
    }

    private int hash(Key key)
    { return (key.hashCode() & 0xffffffff) % M; }

    public Value get(Key key) {
        int i = hash(key);
        for (Node x = st[i]; x != null; x = x.next)
            if (key.equals(x.key)) return (Value) x.val;
        return null;
    }

}
```

array doubling and  
halving code omitted

# Separate-chaining symbol table: Java implementation

---

```
public class SeparateChainingHashST<Key, Value>
{
    private int M = 97;                      // number of chains
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    private static class Node
    {
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        private Node next;
        ...
    }

    private int hash(Key key)
    { return (key.hashCode() & 0xffffffff) % M; }

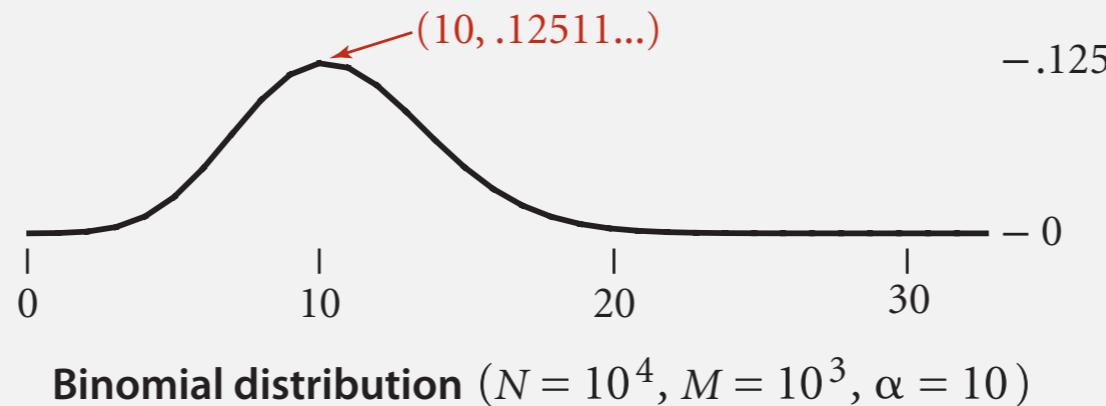
    public void put(Key key, Value val) {
        int i = hash(key);
        for (Node x = st[i]; x != null; x = x.next)
            if (key.equals(x.key)) { x.val = val; return; }
        st[i] = new Node(key, val, st[i]);
    }

}
```

# Analysis of separate chaining

**Proposition.** Under uniform hashing assumption, prob. that the number of keys in a list is within a constant factor of  $N/M$  is extremely close to 1.

**Pf sketch.** Distribution of list size obeys a binomial distribution.



**Consequence.** Number of probes for search/insert is proportional to  $N/M$ .

- $M$  too large  $\Rightarrow$  too many empty chains.
- $M$  too small  $\Rightarrow$  chains too long.
- Typical choice:  $M \sim N/4 \Rightarrow$  constant-time ops.

equals() and hashCode()

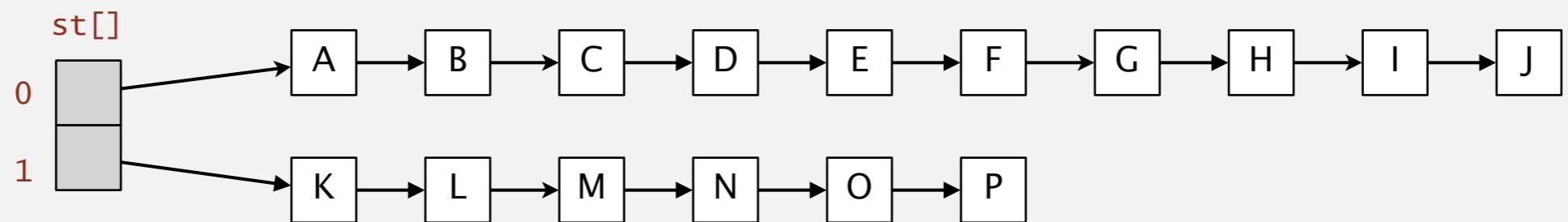
$\uparrow$   
M times faster than  
sequential search

# Resizing in a separate-chaining hash table

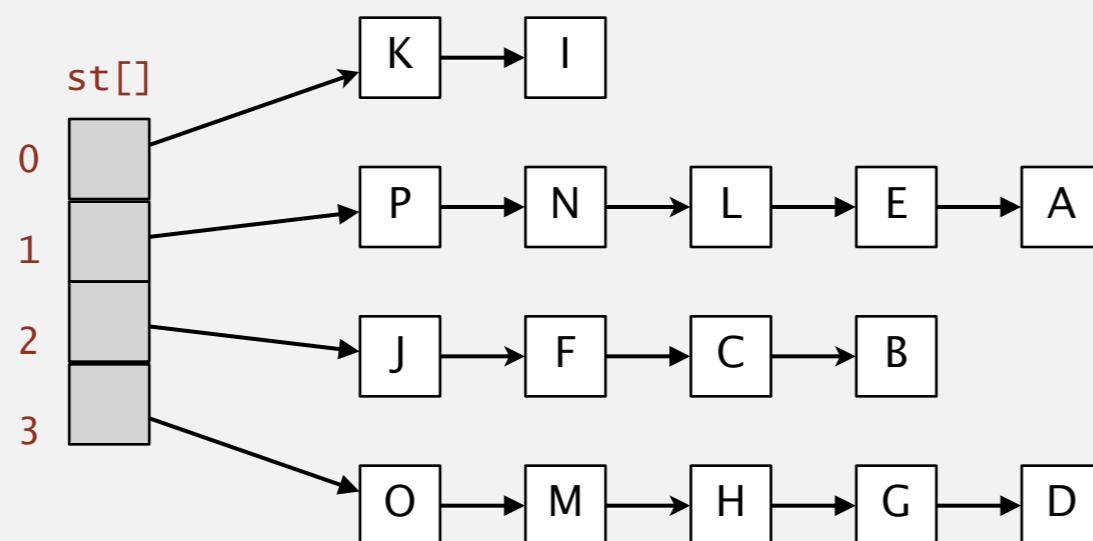
**Goal.** Average length of list  $N / M = \text{constant}$ .

- Double size of array  $M$  when  $N / M \geq 8$ .
- Halve size of array  $M$  when  $N / M \leq 2$ .
- Need to rehash all keys when resizing. ← x.hashCode() does not change  
but hash(x) can change

**before resizing**



**after resizing**

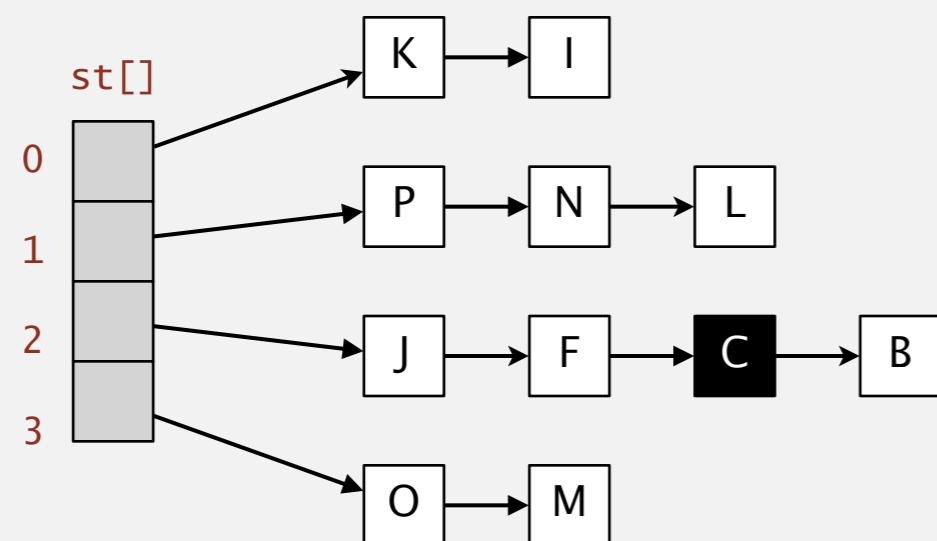


# Deletion in a separate-chaining hash table

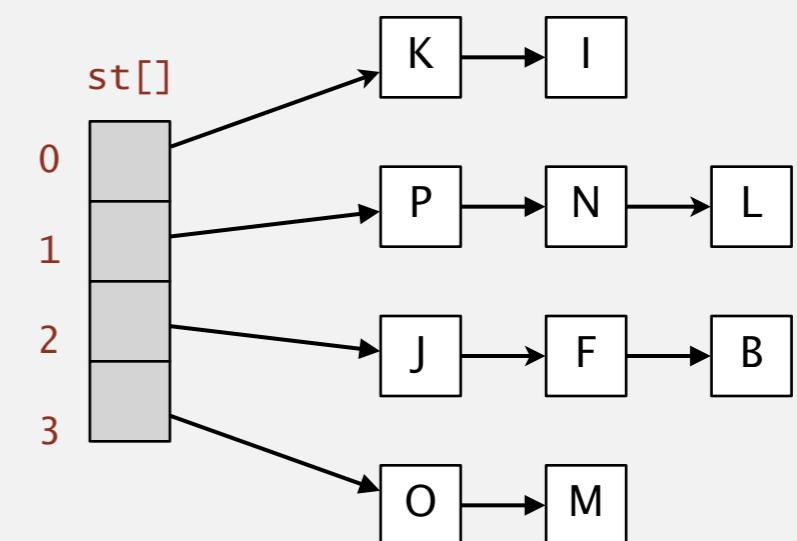
Q. How to delete a key (and its associated value)?

A. Easy: need only consider chain containing key.

**before deleting C**



**after deleting C**



# Symbol table implementations: summary

---

implementation	guarantee			average case			ordered ops?	key interface
	search	insert	delete	search hit	insert	delete		
<b>sequential search (unordered list)</b>	$N$	$N$	$N$	$\frac{1}{2}N$	$N$	$\frac{1}{2}N$		<code>equals()</code>
<b>binary search (ordered array)</b>	$\lg N$	$N$	$N$	$\lg N$	$\frac{1}{2}N$	$\frac{1}{2}N$	✓	<code>compareTo()</code>
<b>BST</b>	$N$	$N$	$N$	$1.39 \lg N$	$1.39 \lg N$	$\sqrt{N}$	✓	<code>compareTo()</code>
<b>red-black BST</b>	$2 \lg N$	$2 \lg N$	$2 \lg N$	$1.0 \lg N$	$1.0 \lg N$	$1.0 \lg N$	✓	<code>compareTo()</code>
<b>separate chaining</b>	$N$	$N$	$N$	3-5 *	3-5 *	3-5 *		<code>equals()</code> <code>hashCode()</code>

\* under uniform hashing assumption

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## 3.4 HASH TABLES

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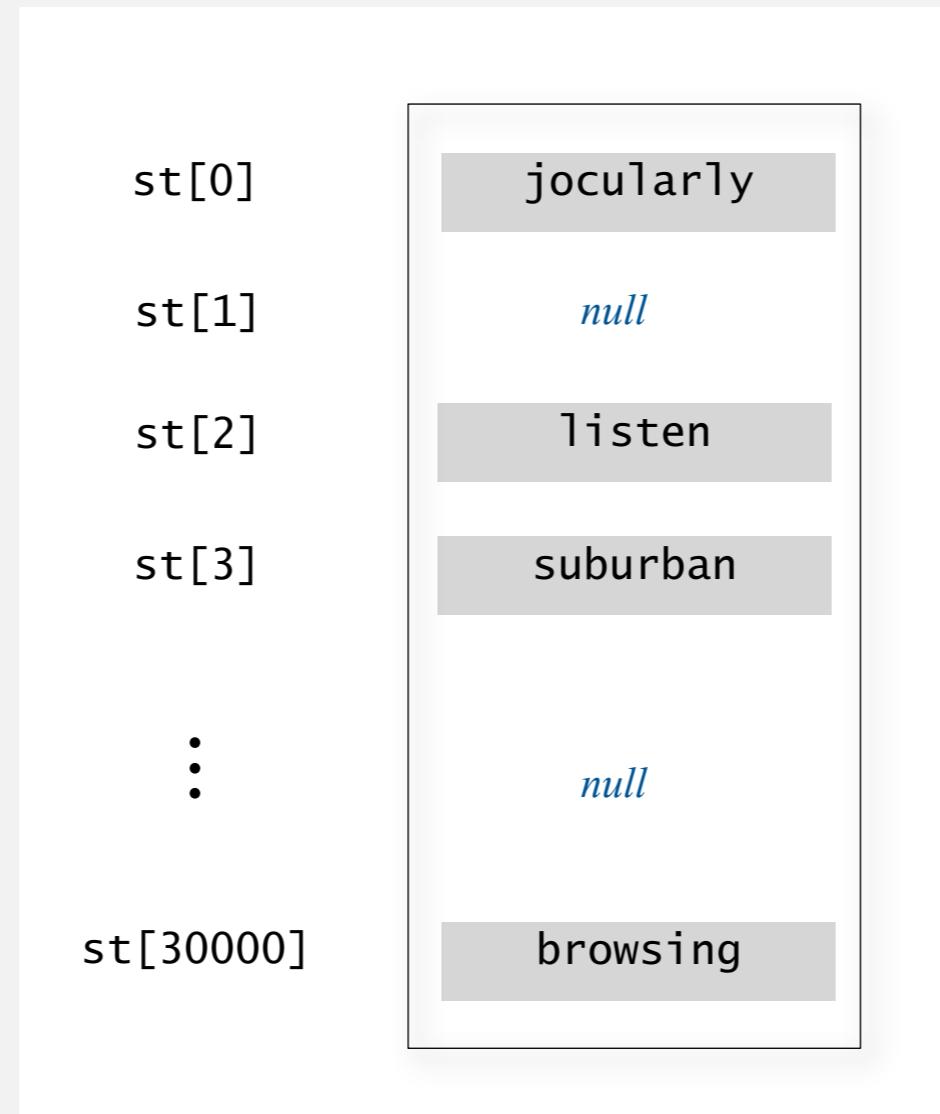
- ▶ *hash functions*
- ▶ *separate chaining*
- ▶ ***linear probing***
- ▶ *context*

# Collision resolution: open addressing

---

Open addressing. [Amdahl-Boehme-Rochester-Samuel, IBM 1953]

When a new key collides, find next empty slot, and put it there.



linear probing ( $M = 30001$ ,  $N = 15000$ )

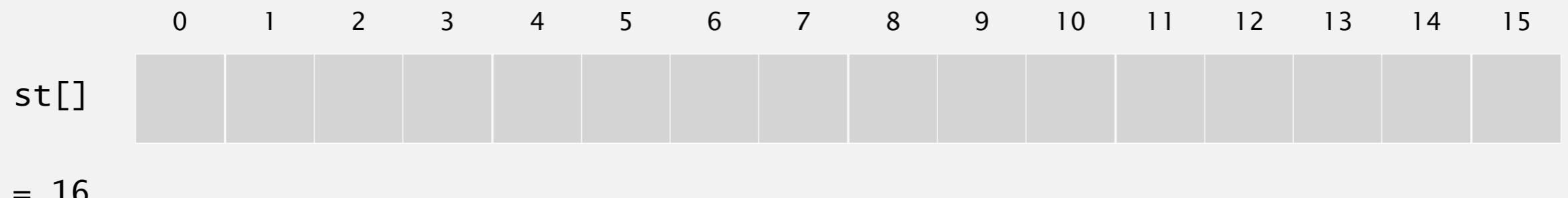
# Linear-probing hash table demo

---

**Hash.** Map key to integer  $i$  between 0 and  $M-1$ .

**Insert.** Put at table index  $i$  if free; if not try  $i+1, i+2, \dots$

**linear-probing hash table**



# Linear-probing hash table demo

---

**Hash.** Map key to integer  $i$  between 0 and  $M-1$ .

**Search.** Search table index  $i$ ; if occupied but no match, try  $i+1$ ,  $i+2$ , etc.

search K

hash(K) = 5

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
st[]	P	M			A	C	S	H	L		E				R	X

$M = 16$

K

search miss  
(return null)

# Linear-probing hash table summary

---

**Hash.** Map key to integer  $i$  between 0 and  $M-1$ .

**Insert.** Put at table index  $i$  if free; if not try  $i+1, i+2, \dots$

**Search.** Search table index  $i$ ; if occupied but no match, try  $i+1, i+2, \dots$

**Note.** Array size  $M$  must be greater than number of key-value pairs  $N$ .

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
st[]	P	M			A	C	S	H	L		E				R	X

$$M = 16$$

# Linear-probing symbol table: Java implementation

```
public class LinearProbingHashST<Key, Value>
{
    private int M = 30001;
    private Value[] vals = (Value[]) new Object[M];
    private Key[] keys = (Key[]) new Object[M];

    private int hash(Key key) { /* as before */ }

    private void put(Key key, Value val) { /* next slide */ }

    public Value get(Key key)
    {
        for (int i = hash(key); keys[i] != null; i = (i+1) % M)
            if (key.equals(keys[i]))
                return vals[i];
        return null;
    }
}
```

array doubling and  
halving code omitted

# Linear-probing symbol table: Java implementation

---

```
public class LinearProbingHashST<Key, Value>
{
    private int M = 30001;
    private Value[] vals = (Value[]) new Object[M];
    private Key[] keys = (Key[]) new Object[M];

    private int hash(Key key) { /* as before */ }

    private Value get(Key key) { /* previous slide */ }

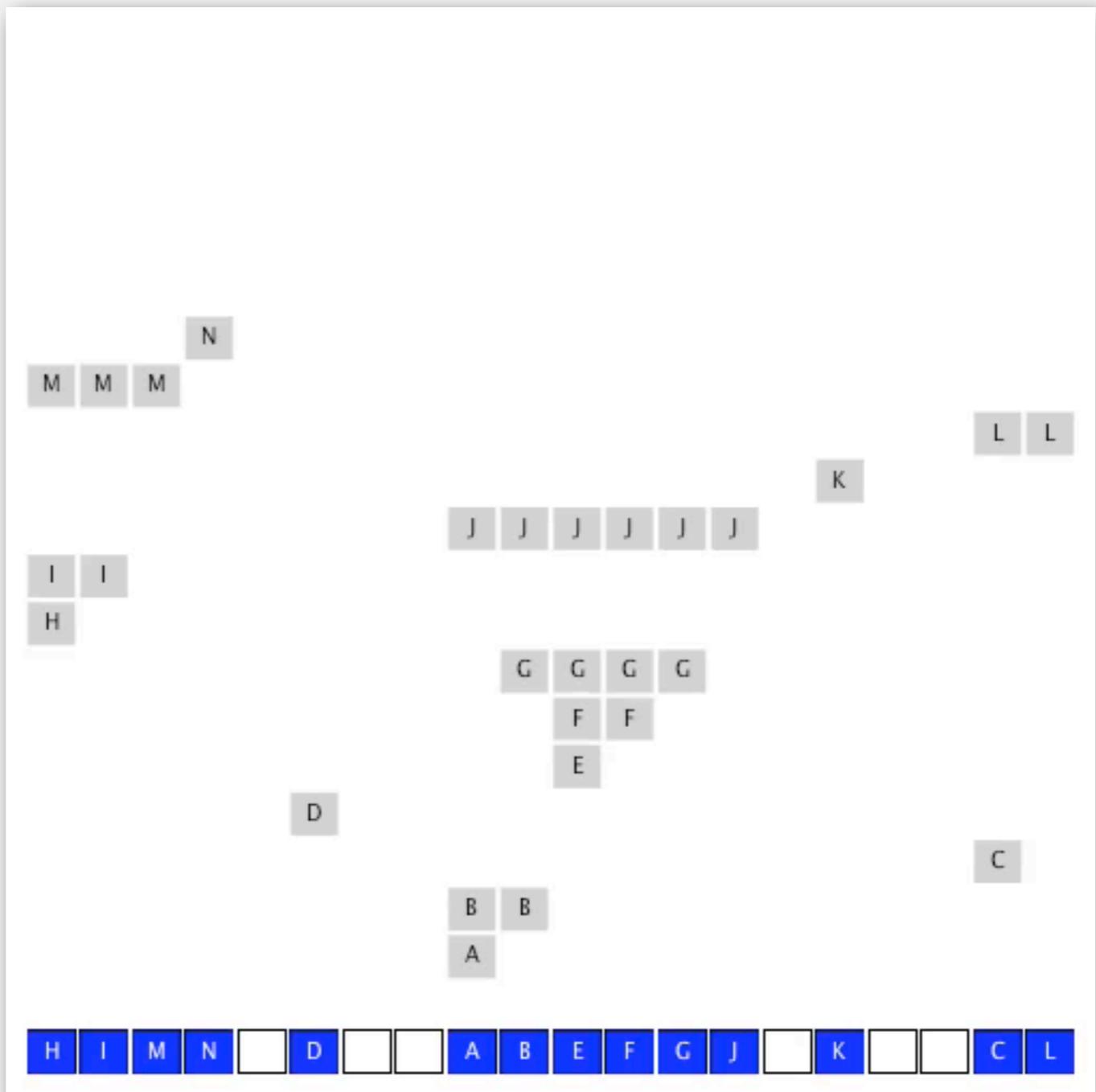
    public void put(Key key, Value val)
    {
        int i;
        for (i = hash(key); keys[i] != null; i = (i+1) % M)
            if (keys[i].equals(key))
                break;
        keys[i] = key;
        vals[i] = val;
    }
}
```

# Clustering

---

**Cluster.** A contiguous block of items.

**Observation.** New keys likely to hash into middle of big clusters.



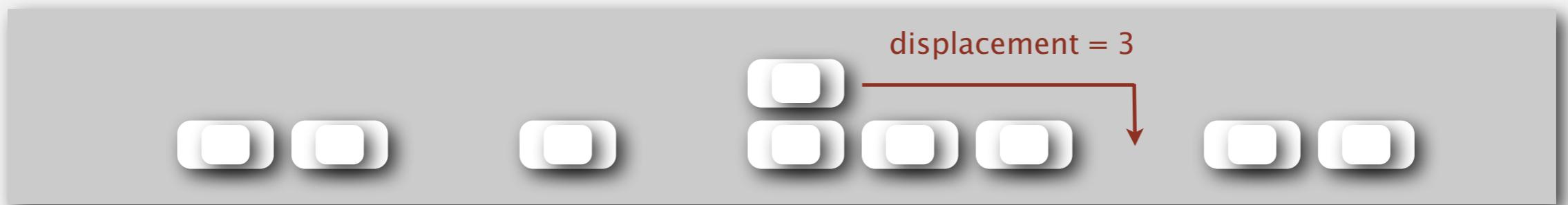
# Knuth's parking problem

---

**Model.** Cars arrive at one-way street with  $M$  parking spaces.

Each desires a random space  $i$ : if space  $i$  is taken, try  $i + 1, i + 2$ , etc.

**Q.** What is mean displacement of a car?



**Half-full.** With  $M/2$  cars, mean displacement is  $\sim 3/2$ .

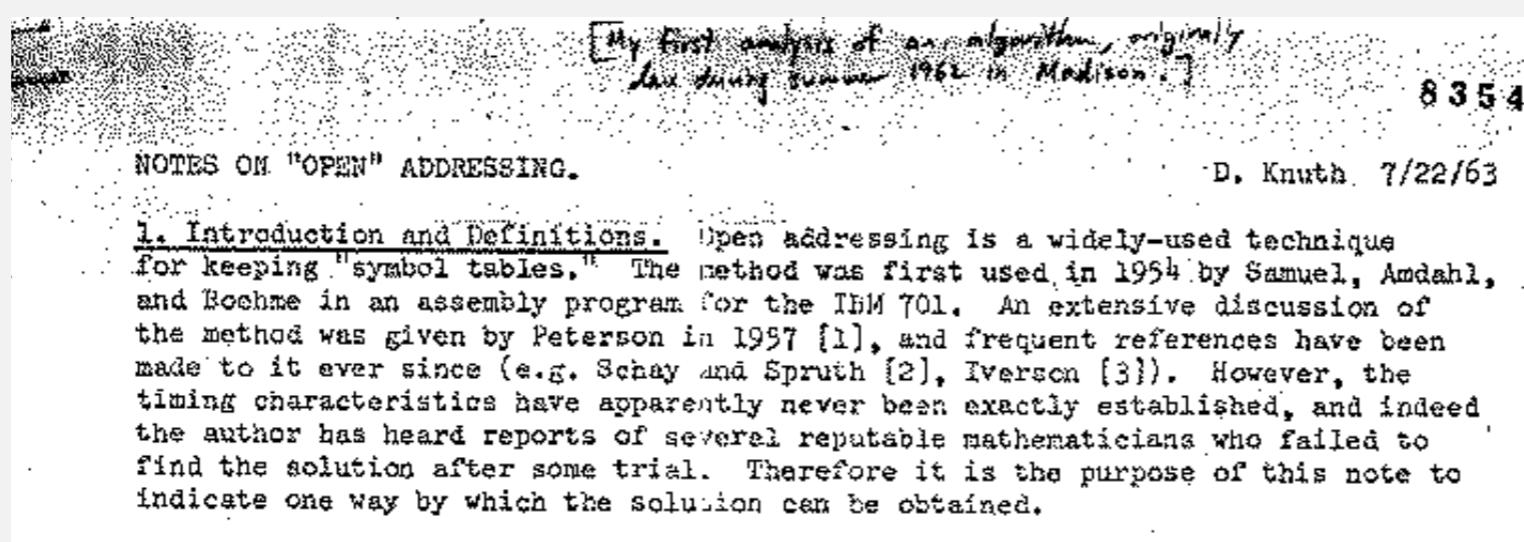
**Full.** With  $M$  cars, mean displacement is  $\sim \sqrt{\pi M / 8}$ .

# Analysis of linear probing

**Proposition.** Under uniform hashing assumption, the average # of probes in a linear probing hash table of size  $M$  that contains  $N = \alpha M$  keys is:

$$\begin{array}{ll} \sim \frac{1}{2} \left( 1 + \frac{1}{1-\alpha} \right) & \sim \frac{1}{2} \left( 1 + \frac{1}{(1-\alpha)^2} \right) \\ \text{search hit} & \text{search miss / insert} \end{array}$$

Pf.



## Parameters.

- $M$  too large  $\Rightarrow$  too many empty array entries.
- $M$  too small  $\Rightarrow$  search time blows up.
- Typical choice:  $\alpha = N/M \sim 1/2.$  ← # probes for search hit is about 3/2  
# probes for search miss is about 5/2

# Resizing in a linear-probing hash table

---

**Goal.** Average length of list  $N / M \leq \frac{1}{2}$ .

- Double size of array  $M$  when  $N / M \geq \frac{1}{2}$ .
- Halve size of array  $M$  when  $N / M \leq \frac{1}{8}$ .
- Need to rehash all keys when resizing.

**before resizing**

	0	1	2	3	4	5	6	7
keys[]		E	S		R	A		
vals[]		1	0		3	2		

**after resizing**

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
keys[]				A		S			E				R			
vals[]					2	0			1				3			

# Deletion in a linear-probing hash table

Q. How to delete a key (and its associated value)?

A. Requires some care: can't just delete array entries.

**before deleting S**

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
keys[]	P	M			A	C	S	H	L		E			R	X	
vals[]	10	9			8	4	0	5	11		12			3	7	

**after deleting S ?**

doesn't work, e.g., if  $\text{hash}(H) = 4$



	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
keys[]	P	M			A	C		H	L		E			R	X	
vals[]	10	9			8	4		5	11		12			3	7	

# ST implementations: summary

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<b>red-black BST</b>	$2 \lg N$	$2 \lg N$	$2 \lg N$	$1.0 \lg N$	$1.0 \lg N$	$1.0 \lg N$	✓	<code>compareTo()</code>
<b>separate chaining</b>	$N$	$N$	$N$	3-5 *	3-5 *	3-5 *		<code>equals()</code> <code>hashCode()</code>
<b>linear probing</b>	$N$	$N$	$N$	3-5 *	3-5 *	3-5 *		<code>equals()</code> <code>hashCode()</code>

\* under uniform hashing assumption

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- ▶ *linear probing*
- ▶ **context**

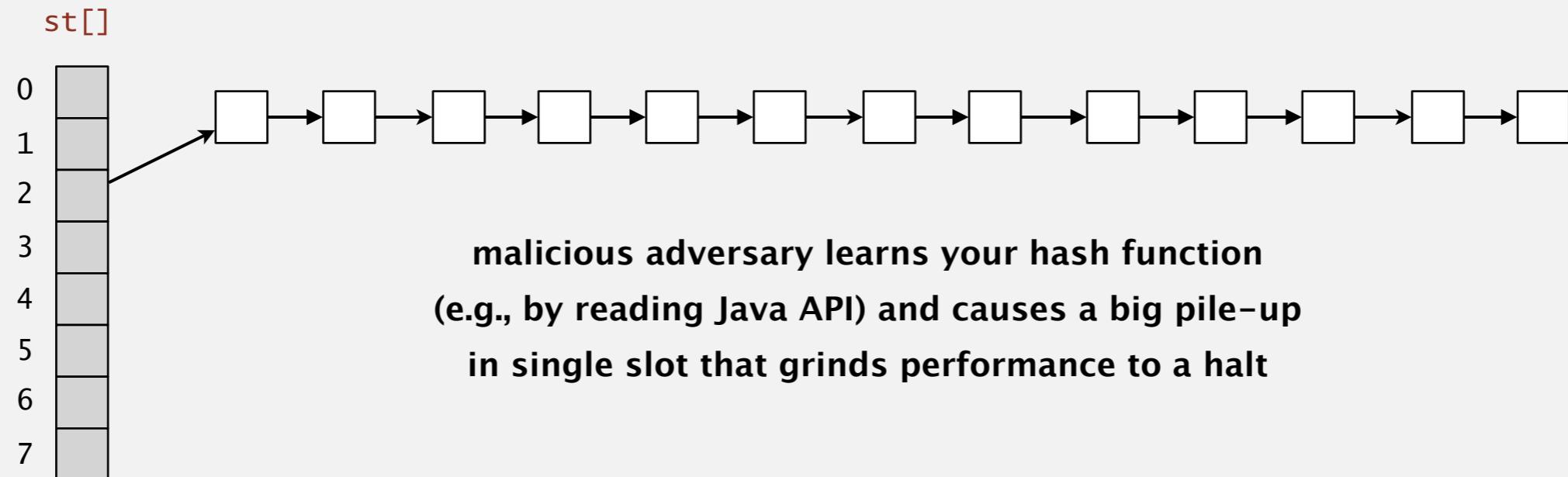
## War story: algorithmic complexity attacks

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Q. Is the uniform hashing assumption important in practice?

A. Obvious situations: aircraft control, nuclear reactor, pacemaker.

A. Surprising situations: **denial-of-service** attacks.



Real-world exploits. [Crosby-Wallach 2003]

- Bro server: send carefully chosen packets to DOS the server, using less bandwidth than a dial-up modem.
- Perl 5.8.0: insert carefully chosen strings into associative array.
- Linux 2.4.20 kernel: save files with carefully chosen names.

# War story: algorithmic complexity attacks

## A Java bug report.

Jan Lieskovsky 2011-11-01 10:13:47 EDT	Description
Julian Wälde and Alexander Klink reported that the <code>String.hashCode()</code> hash function is not sufficiently collision resistant. <code>hashCode()</code> value is used in the implementations of <code>HashMap</code> and <code>Hashtable</code> classes:	
<a href="http://docs.oracle.com/javase/6/docs/api/java/util/HashMap.html">http://docs.oracle.com/javase/6/docs/api/java/util/HashMap.html</a>	
<a href="http://docs.oracle.com/javase/6/docs/api/java/util/Hashtable.html">http://docs.oracle.com/javase/6/docs/api/java/util/Hashtable.html</a>	
A specially-crafted set of keys could trigger hash function collisions, which can degrade performance of <code>HashMap</code> or <code>Hashtable</code> by changing hash table operations complexity from an expected/average $O(1)$ to the worst case $O(n)$ . Reporters were able to find colliding strings efficiently using equivalent substrings and meet in the middle techniques.	
This problem can be used to start a denial of service attack against Java applications that use untrusted inputs as <code>HashMap</code> or <code>Hashtable</code> keys. An example of such application is web application server (such as tomcat, see <a href="#">bug #750521</a> ) that may fill hash tables with data from HTTP request (such as GET or POST parameters). A remote attack could use that to make JVM use excessive amount of CPU time by sending a POST request with large amount of parameters which hash to the same value.	
This problem is similar to the issue that was previously reported for and fixed in e.g. perl:	
<a href="http://www.cs.rice.edu/~scrosby/hash/CrosbyWallach_UseNixSec2003.pdf">http://www.cs.rice.edu/~scrosby/hash/CrosbyWallach_UseNixSec2003.pdf</a>	

# Algorithmic complexity attack on Java

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**Goal.** Find family of strings with the same hash code.

**Solution.** The base-31 hash code is part of Java's string API.

key	hashCode()
"Aa"	2112
"BB"	2112

key	hashCode()
"AaAaAaAa"	-540425984
"AaAaAaBB"	-540425984
"AaAaBBAa"	-540425984
"AaAaBBBB"	-540425984
"AaBBAaAa"	-540425984
"AaBBAaBB"	-540425984
"AaBBBBAa"	-540425984
"AaBBBBBB"	-540425984

key	hashCode()
"BBAaAaAa"	-540425984
"BBAaAaBB"	-540425984
"BBAaBBAa"	-540425984
"BBAaBBBB"	-540425984
"BBBBAaAa"	-540425984
"BBBBAaBB"	-540425984
"BBBBBBAA"	-540425984
"BBBBBBBB"	-540425984

**$2^N$  strings of length  $2N$  that hash to same value!**

## Diversion: one-way hash functions

---

**One-way hash function.** "Hard" to find a key that will hash to a desired value (or two keys that hash to same value).

**Ex.** MD4, MD5, SHA-0, SHA-1, SHA-2, WHIRLPOOL, RIPEMD-160, ....

known to be insecure

```
String password = args[0];
MessageDigest sha1 = MessageDigest.getInstance("SHA1");
byte[] bytes = sha1.digest(password);

/* prints bytes as hex string */
```

**Applications.** Digital fingerprint, message digest, storing passwords.

**Caveat.** Too expensive for use in ST implementations.

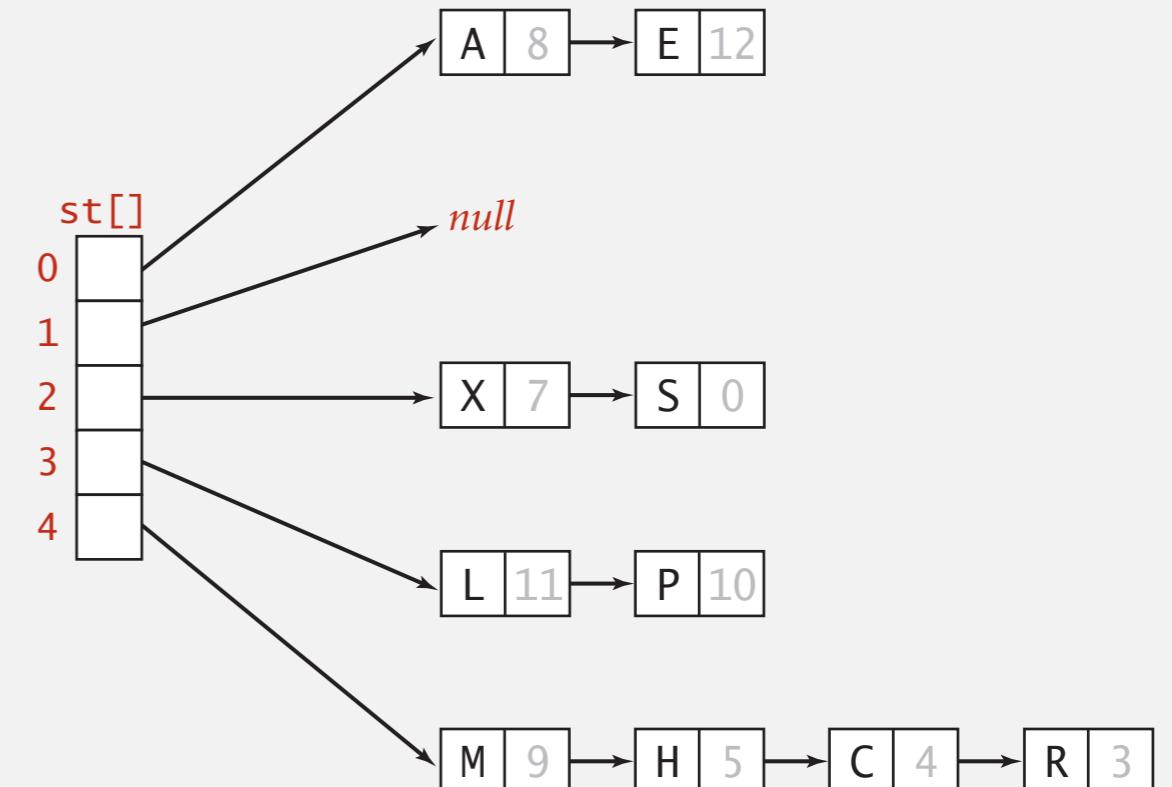
# Separate chaining vs. linear probing

## Separate chaining.

- Performance degrades gracefully.
- Clustering less sensitive to poorly-designed hash function.

## Linear probing.

- Less wasted space.
- Better cache performance.



keys[]	P	M			A	C	S	H	L		E			R	X
vals[]	10	9			8	4	0	5	11		12			3	7

# Hashing: variations on the theme

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Many improved versions have been studied.

## Two-probe hashing. [ separate-chaining variant ]

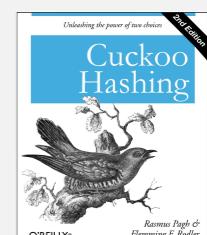
- Hash to two positions, insert key in shorter of the two chains.
- Reduces expected length of the longest chain to  $\log \log N$ .

## Double hashing. [ linear-probing variant ]

- Use linear probing, but skip a variable amount, not just 1 each time.
- Effectively eliminates clustering.
- Can allow table to become nearly full.
- More difficult to implement delete.

## Cuckoo hashing. [ linear-probing variant ]

- Hash key to two positions; insert key into either position; if occupied, reinsert displaced key into its alternative position (and recur).
- Constant worst-case time for search.



# Hash tables vs. balanced search trees

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## Hash tables.

- Simpler to code.
- No effective alternative for unordered keys.
- Faster for simple keys (a few arithmetic ops versus  $\log N$  compares).
- Better system support in Java for strings (e.g., cached hash code).

## Balanced search trees.

- Stronger performance guarantee.
- Support for ordered ST operations.
- Easier to implement `compareTo()` correctly than `equals()` and `hashCode()`.

## Java system includes both.

- Red-black BSTs: `java.util.TreeMap`, `java.util.TreeSet`.
- Hash tables: `java.util.HashMap`, `java.util.IdentityHashMap`.