

**Student Solutions Manual and Study Guide for  
Discrete Mathematics with Applications, 3rd Edition  
by Susanna S. Epp**

**ERRATA**

<b>LOCATION</b>	<b>CORRECTION</b>
<b>1 – 1.1 #15</b>	The heading for the sixth column should be “ $\sim(p \wedge q) \vee (p \vee q)$ .”
<b>5 – 1.3 #9</b>	Line 1: In column 7, change T to F and delete that row 1 is critical. Line 2: In column 7, change F to T and add that row 2 is critical. Row 4 is also critical. The first words of the explanation should say: “Row 3 of the truth table shows...”
<b>13 – Answers #15</b>	Change to “ $p \wedge \sim q$ ”
<b>15 – 2.1 #18d</b>	Change “ $\exists x$ ” to “ $\exists s$ ”.
<b>26 – 3.3 #9</b>	Should be: “Yes, because $2a \cdot 34b = 4(17ab)$ and $17ab$ is an integer since $a$ and $b$ are integers and products of integers are integers.”
<b>28 – 3.4 #18</b>	Line 2: Equation should be “ $96m + 36 + 4 = 12(8m + 3) + 4$ ”.
<b>39 – Review #18</b>	Change “there exists” to “there exist”.
<b>43 – 4.1 #6</b>	Line 1: Change “ $f_3 = \lfloor 3/4 \rfloor \cdot 4 = 0 \cdot 4 = 4$ ” to “ $f_3 = \lfloor 3/4 \rfloor \cdot 4 = 0 \cdot 4 = 0$ ”.
<b>44 – 4.1 #15</b>	In line 1, change the formula to “ $a_n = (-1)^{n-1} (n-1/n)$ ”, and in line 2 change the formula to “ $a_n = (-1)^n (n/n+1)$ ”
<b>51 – 4.4 #21</b>	This solution is missing. It is given below this table.
<b>52 – 4.4 #24</b>	Last line: Change “these two” to “these three”.
<b>65 – 5.3 #39d</b>	Change line 2 to “ $\{1, 2, 5, 6\} = \{1, 2\} \cup \{7, 8\} = \{1, 2, 7, 8\}$ ”.
<b>72 – 6.1 #33</b>	In line 10, change “ $m - (k+1) + 1$ ” to “ $(k+1) - m + 1$ ”.
<b>72 – 6.2 #12b</b>	Line 5: Change “Step 6 is to choose the first...” to “Step 6 is to choose the last...”. Line 6: Change “2 through (which equals 14) There are $14 - 2 + 1 = 11...$ ” to “2 through E (which equals 14). There are $14 - 2 + 1 = 13...$ ”. Line 7: Change “ $10 \cdot 16 \cdot 16 \cdot 16 \cdot 11 = 450,560$ ” to “ $10 \cdot 16 \cdot 16 \cdot 16 \cdot 16 \cdot 13 = 8,519,680$ ”.
<b>79 – 6.7 #9</b>	Change all eight minus signs to plus signs.
<b>80 – 6.7 #18</b>	Line 1: Change “ $a = 5$ and $b = -1$ ” to “ $a = 1$ and $b = 2$ ”.
<b>83 – 6.9 #3b</b>	Line 3: Change “Then the probability” to “The event”.
<b>83 – 6.9 #6c</b>	Line 3: Change “42.8%” to “42.9%”.
<b>85 – 6.9 #24b</b>	Assuming that the manuscript contains 1000 typographical errors, the expected number of missed errors is $(1000) \cdot (0.018) = 18$ .
<b>86 – 6.9 #30d(i)</b>	Change “4.88%” to “0.488%”.
<b>96 – 7.3 #21</b>	Add the word “dividing” in the second sentence. So the second sentence should begin “The reason is that in the long-division process of dividing 5.0000... by 20483,...”
<b>119 – 8.4 #27</b>	Last line on the page: Change to “Hence $M(k) = 91$ [as was to be

	<i>shown].</i> "
<b>131 – 9.3 #3b</b>	Change the equation to " $(8\text{cm}^3)/\text{cm}^3 = 8$ ".
<b>135 – 9.5 #15</b>	Line 4: Change "Then" to "Then all quantities are positive, and so".
<b>149 – 10.4 #33</b>	Line 2: Change " $as + bt = 1$ " to "there exist integers $s$ and $t$ such that $as + bt = 1$ ".
<b>160 – 11.1 #24c</b>	Top line of pictures, second from left: Add an edge from $v_1$ to $v_3$ . Top line of pictures, third from left: Add an edge from $v_2$ to $v_3$ .
<b>176 – 12.1 #9</b>	Add a right parenthesis at the end of this expression.

#### Solution for Section 4.4, exercise 21

*Proof 1:* Let  $r$  be any rational number. [We must show that there exists an integer  $m$  such that  $m \leq r < m + 1$ .]

*Case 1* ( $r$  is an integer): In this case  $r \leq r < r + 1$ , and so there exists an integer  $m$  (namely  $r$ ) such that  $m \leq r < m + 1$ .

*Case 2* ( $r$  is not an integer and  $r > 0$ ): In this case let  $S$  be the set of all integers  $n$  such that  $r < n$ . That is,  $S = \{n \in \mathbf{Z} \mid r < n\}$ . By the result of exercise 20, there is some integer that is greater than  $r$ , and so  $S$  has one or more elements. Also, because  $r > 0$ , every element of  $S$  is greater than 0 (by the transitive property of order). Therefore, by the well-ordering principle for the integers,  $S$  has a least element. Call it  $k$ . Then  $k - 1$  is not in  $S$ , and so  $k - 1 \leq r < k$ . Let  $m = k - 1$ . Then  $m \leq r < m + 1$ .

*Case 3* ( $r$  is not an integer and  $r < 0$ ): In this case  $-r > 0$ , and so, by case 2, there exists an integer  $k - 1$  such that  $k - 1 \leq -r < k$ . Multiply all parts of this inequality by  $-1$  to obtain  $-(k - 1) \geq r > -k$ , or, equivalently,  $-k < r \leq -k + 1$ . Because  $r$  is not an integer,  $r \neq -k + 1$ , and so  $-k < r < -k + 1$ . Let  $m = -k$ . Then  $m \leq r < m + 1$ .

Hence in all three cases there exists an integer  $m$  such that  $m \leq r < m + 1$  [as was to be shown].

*Proof 2:* Let  $r$  be any rational number. [We must show that there exists an integer  $m$  such that  $m \leq r < m + 1$ .] Let  $S$  be the set of all integers  $n$  such that  $r < n$ . That is,  $S = \{n \in \mathbf{Z} \mid r < n\}$ . By the result of exercise 20, there is some integer that is greater than  $r$ , and so  $S$  has one or more elements. Also, every element of  $S$  is greater than some integer. The reason is that because  $-r$  is also rational, the result of exercise 20 implies that there is an integer  $t$  such that  $-r < t$ . Multiplying both sides of this inequality by  $-1$  gives that  $r > -t$ , and thus that there is an integer,  $-t$ , that is less than  $r$ . Hence, by the transitive property of order, every element of  $S$  is greater than the integer  $-t$ . It follows by the well-ordering principle for the integers that  $S$  has a least element. Call it  $k$ . Then  $k - 1$  is not in  $S$ , and so  $k - 1 \leq r < k$ . Let  $m = k - 1$ . Then  $m \leq r < m + 1$  [as was to be shown].